# steppyngstounes: Iterators for Python 

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## Contents

1 Dependencies ..... 3
1.1 Using ..... 3
1.2 Testing ..... 4
1.3 Documenting ..... 4
2 Installing ..... 4
3 Testing ..... 4
4 Building the Documentation ..... 4
5 Support ..... 4
6 API ..... 5
6.1 steppyngstounes ..... 5
7 Terms of Use ..... 29
Python Module Index ..... 31
Index ..... 32
steppyngstounes / 'step in, stornz /

1. pl. n. [Middle English] Stones used as steps of a stairway; also, stones in a stream used for crossing. ${ }^{1}$
... while at Calais in 1474 we find 40 'steppyngstounes' bought for the stairways of the town. ${ }^{2}$
2. n. [chiefly Pythonic] A package that provides iterators for advancing from start to stop, subject to algorithms that depend on user-defined value or error.
[^0]```
        Testing and Coverage
and-coverage.yml)
```


## Linting and Spelling passing

```
and-spelling.yml)
contributors 6
```

```
for step in range(steps):
```

for step in range(steps):
do_something(step)

```
    do_something(step)
```

        failing
                (https://github.com/usnistgov/steppyngstounes/actions/workflows/testing-
    (https://github.com/usnistgov/steppyngstounes/actions/workflows/build-docs.yml)
(https://github.com/usnistgov/steppyngstounes/actions/workflows/linting-
(https://github.com/guyer/steppyngstounes)
code quality A
(https://www.codacy.com/gh/guyer/steppyngstounes/dashboard?utm_source=github.com\&utm_medium=referral\&utm_content=
Computations that evolve in time or sweep a variable often boil down to a control loop like
or

```
t = 0
while t < totaltime:
    t += dt
    do_something(dt)
```

which works well enough, until the size of the steps needs to change. This can be to save or plot results at some fixed points, or because the computation becomes either harder or easier to perform. The control loop then starts to dominate the script, obscuring the interesting parts of the computation, particularly as different edge cases are accounted for.

Packages like odeint (https://docs.scipy.org/doc/scipy/reference/generated/scipy.integrate.odeint.html) address many of these issues, but do so through callback functions, which effectively turn the computation of interest inside out, again obscuring the interesting bits. Further, because they are often tailored for applications like solving ordinary differential equations, applying them to other stepping problems, even solving partial differential equations (https://www.ctcms.nist.gov/fipy), can be rather opaque.

The steppyngstounes package is designed to retain the simplicity of the original control loop, while allowing great flexibility in how steps are taken and automating all of the aspects of increasing and decreasing the step size.

A steppyngstounes control loop can be as simple as

```
from steppyngstounes import FixedStepper
for step in FixedStepper(start=0., stop=totaltime, size=dt):
    do_something(step.size)
    _ = step.succeeded()
```

which replicates the while construct above, but further ensures that total ime is not overshot if it isn't evenly divisible by $d t$.

Attention: The call to succeeded () informs the Stepper to advance, otherwise it will iterate on the same step indefinitely.

Rather than manually incrementing the control variable (e.g., $t$ ), the values of the control variable before and after the step are available as the $S t e p$ attributes begin and end. The attribute size is a shorthand for step.end - step. begin.

If the size of the steps should be adjusted by some characteristic of the calculation, such as the change in the value since the last solution, the error (normalized to 1) can be passed to succeeded (), causing the Stepper to advance (possibly adjusting the next step size) or to retry the step with a smaller step size.

```
from steppyngstounes import SomeStepper
old = initial_condition
for step in SomeStepper(start=0., stop=totaltime, size=dt):
    new = do_something_else(step.begin, step.end, step.size)
    err = (new - old) / scale
    if step.succeeded(error=err):
        old = new
        # do happy things
    else:
        # do sad things
```

A hierarchy of Stepper iterations enables saving or plotting results at fixed, possibly irregular, points, while allowing an adaptive Stepper to find the most efficient path between those checkpoints.

```
from steppyngstounes import CheckpointStepper, SomeStepper
old = initial_condition
for checkpoint in CheckpointStepper(start=0.,
    stops=[1e-3, 1, 1e3, 1e6]):
    for step in SomeStepper(start=checkpoint.begin,
                stop=checkpoint.end,
                size=checkpoint.size):
        new = do_something_else(step.begin, step.end, step.size)
        err = (new - old) / scale
        if step.succeeded(error=err):
            old = new
            # do happy things
        else:
            # do sad things
    save_or_plot()
    _ = checkpoint.succeeded()
```

A variety of stepping algorithms are described and demonstrated in the documentation of the individual steppyngstounes classes.

## 1 Dependencies

### 1.1 Using

- numpy (https://numpy.org/)
- scipy (https://scipy.org/)


### 1.2 Testing

- pytest (https://pytest.org/)


### 1.3 Documenting

- sphinx (https://www.sphinx-doc.org/) $>=3.1$
- matplotlib (https://matplotlib.org/)


## 2 Installing

```
$ python setup.py install
```


## 3 Testing

```
$ pytest
```


## 4 Building the Documentation

```
$ python setup.py build_sphinx
```

If the figures do not update

```
$ touch docs/_autosummary/*.rst
```

and repeat.
If the documentation seems not to build correctly in other respects:

```
$ python setup.py build_sphinx --all-files --fresh-env
```

Documentation can be found in STEPPYNGSTOUNES/build/sphinx/html.

## 5 Support

For help using this package, file an issue (https://github.com/guyer/steppyngstounes/issues) on the GitHub repository (https://github.com/guyer/steppyngstounes). Contributions are welcome via pull request (https://github.com/guyer/steppyngstounes/pulls).

## 6 API

Description of specific Stepper classes:

```
steppyngstounes
```


## 6.1 steppyngstounes

## Modules

```
steppyngstounes.checkpointStepper
steppyngstounes.fixedStepper
steppyngstounes.parsimoniousStepper
steppyngstounes.pidStepper
steppyngstounes.pseudoRKQSStepper
steppyngstounes.scaledStepper
steppyngstounes.sequenceStepper
steppyngstounes.stepper
```


## steppyngstounes.checkpointStepper

## Classes

```
class steppyngstounes.checkpointStepper.CheckpointStepper(start, stops, stop=inf,
                                    inclusive=False,
                                    record=False)
```

Bases: Stepper
Stepper that stops at fixed points.

## Parameters

- start (float) - Beginning of range to step over.
- stops (iterable of float)-Desired checkpoints.
- stop (float, optional) - Finish of range to step over (default np.inf). In the event that any of stops exceed stop, the stepper will terminate at stop. A step will not be taken to stop otherwise (clear?).
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import CheckpointStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old । / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> stepper = CheckpointStepper(start=0., stop=totaltime, inclusive=True,
... stops=10.**np.arange(-5, 5), record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
...
... _ = step.succeeded(value=new)
```

```
>>>}s="{} succesful steps in {} attempts
>>> print(s.format (stepper.successes.sum(),
... len(stepper.steps)))
10 succesful steps in 10 attempts
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

As this stepper doesn't use the error, we don't expect the post hoc error to satisfy the tolerance.

## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

10 successful CheckpointStepper steps and trajectory of 10 attempts


## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.
property steps
ndarray of values of the control variable attempted so far.

```
succeeded (step, value=None, error=None)
```

Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional)- User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which $S t e p p e r$ is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool
property successes
ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.fixedStepper

## Classes

class steppyngstounes.fixedStepper.FixedStepper (start, stop, size=None, minStep=None, inclusive $=$ False, record $=$ False , limiting $=$ False )

Bases: Stepper
Stepper that takes steps of constant size.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- size (float) - Desired step size.
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import FixedStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old | / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> stepper = FixedStepper(start=0., stop=totaltime, inclusive=True,
... size=3., record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
...
... - = step.succeeded(value=new)
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
... len(stepper.steps)))
3 3 5 \text { succesful steps in 335 attempts}
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

As this stepper doesn't use the error, we don't expect the post hoc error to satisfy the tolerance.

## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

335 successful FixedStepper steps and trajectory of 335 attempts


## Return type

Step

## Raises

StopIteration - If there are no further steps to take
property sizes
ndarray of the step size at each step attempt.
property steps
ndarray of values of the control variable attempted so far.
succeeded (step, value $=$ None, error $=$ None $)$
Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional)-User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool

## property successes

ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.parsimoniousStepper

## Classes

class steppyngstounes.parsimoniousStepper.ParsimoniousStepper (start, stop, $N$, minStep $=0.0$, inclusive $=$ False, scale $=$ 'dl', minsteps $=4$, maxinitial=11)
Bases: Stepper
Non-monotonic stepper that samples sparsely explored regions
Computes the function where the curvature is highest and where not many points have been computed.

Note: By its nature, this Stepper must record.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- $\mathbf{N}(i n t)$ - Number of points to sample.
- minStep (float) - Smallest step to allow (default (stop - start) * eps (https://numpy.org/doc/stable/reference/generated/numpy.finfo.html)).
- inclusive (bool) - Whether to include an evaluation at start (default False)
- scale (str) - Parameter to indicate whether to scale by value "dy" or arc length "dl" (default "dl").
- minsteps (int) - Minimum number of steps to take (default 4).
- maxinitial (int) - The maximum number of even steps to take before adapting (default 11).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import ParsimoniousStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old I / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> stepper = ParsimoniousStepper(start=0., stop=totaltime, inclusive=True,
... N=50)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
...
... - = step.succeeded(value=new)
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
... len(stepper.steps)))
50 succesful steps in 50 attempts
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

As this stepper doesn't use the error, we don't expect the post hoc error to satisfy the tolerance.
50 successful ParsimoniousStepper steps and trajectory of 50 attempts


## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.

## property steps

ndarray of values of the control variable attempted so far.
succeeded (step, value $=$ None, error $=$ None)
Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional) - User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool

## property successes

ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.pidStepper

## Classes

class steppyngstounes.pidStepper.PIDStepper (start, stop, size=None, minStep $=$ None, inclusive=False, record $=$ False, limiting=True, proportional $=0.075$, integral $=0.175$, derivative $=0.01$ )

Bases: Stepper
Adaptive stepper using a PID controller.
Calculates a new step as

$$
\Delta_{n+1}=\left(\frac{e_{n-1}}{e_{n}}\right)^{k_{P}}\left(\frac{1}{e_{n}}\right)^{k_{I}}\left(\frac{e_{n-1}^{2}}{e_{n} e_{n-2}}\right)^{k_{D}} \Delta_{n}
$$

where $\Delta_{n}$ is the step size for step $n$ and $e_{n}$ is the error at step $n$. $k_{P}$ is the proportional coefficient, $k_{I}$ is the integral coefficient, and $k_{D}$ is the derivative coefficient.

On failure, retries with

$$
\Delta_{n}=\min \left(\frac{1}{e_{n}}, 0.8\right) \Delta_{n}
$$

Based on:

```
@article{PIDpaper,
    author = {A. M. P. Valli and G. F. Carey and A. L. G. A. Coutinho},
    title = {Control strategies for timestep selection in finite
        element simulation of incompressible flows and
        coupled reaction-convection-diffusion processes},
    journal = {Int. J. Numer. Meth. Fluids},
    volume = 47,
    year = 2005,
    pages = {201-231},
    doi = {10.1002/fld.805},
}
```


## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- size (float) - Suggested step size to try (default None).
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).
- limiting (bool) - Whether to prevent error from exceeding 1 (default True).
- minStep (float) - Smallest step to allow (default (stop - start) * eps (https://numpy.org/doc/stable/reference/generated/numpy.finfo.html)).
- proportional (float) - PID control $k_{P}$ coefficient (default 0.075).
- integral (float) - PID control $k_{I}$ coefficient (default 0.175 ).
- derivative (float) - PID control $k_{D}$ coefficient (default 0.01 ).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import PIDStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old | / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> old = -1.
>>> stepper = PIDStepper(start=0., stop=totaltime, inclusive=True,
... record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
. . .
... error = abs(new - old) / errorscale
...
... if step.succeeded(value=new, error=error):
... old = new
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
... len(stepper.steps)))
256 succesful steps in 274 attempts
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

Check that the post hoc error satisfies the desired tolerance.

```
>>> print(max(errors) < 1.)
True
```


## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded ().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.

## property steps

ndarray of values of the control variable attempted so far.
succeeded (step, value=None, error=None)
Test if step was successful.
Stores data about the last step.

## Parameters

256 successful PIDStepper steps and trajectory of 274 attempts


- step (Step) - The step to test.
- value (float, optional) - User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool
property successes
ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.pseudoRKQSStepper

## Classes

class steppyngstounes.pseudoRKQSStepper.PseudoRKQSStepper (start, stop, size=None, minStep $=$ None, inclusive $=$ False, , record $=$ False, limiting $=$ True, safety $=0.9$, pgrow $=-0.2$, pshrink $=-0.25$, maxgrow $=5$, minshrink $=0.1$ )
Bases: Stepper
Pseudo-Runge-Kutta adaptive stepper.
Based on the rkqs (Runge-Kutta "quality-controlled" stepper) algorithm of Numerical Recipes in C: 2nd Edition, Section 16.2.

Not really appropriate, since we're not doing the $r k c k$ Runge-Kutta steps in the first place, but works OK.
Calculates a new step as

$$
\Delta_{n+1}=\min \left[S\left(e_{n}\right)^{P_{\text {grow }}}, f_{\max }\right] \Delta_{n}
$$

where $\Delta_{n}$ is the step size for step $n$ and $e_{n}$ is the error at step $n$. $S$ is the safety factor, $P_{\text {grow }}$ is the growth exponent, and $f_{\text {max }}$ is the maximum factor to grow the step size.
On failure, retries with

$$
\Delta_{n}=\max \left[S\left(e_{n}\right)^{P_{\text {shrink }}}, f_{\min }\right] \Delta_{n}
$$

where $P_{\text {shrink }}$ is the shrinkage exponent and $f_{\min }$ is the minimum factor to shrink the stepsize.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- size (float) - Suggested step size to try (default None).
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).
- limiting (bool) - Whether to prevent error from exceeding 1 (default True).
- minStep (float) - Smallest step to allow (default (stop - start) * eps (https://numpy.org/doc/stable/reference/generated/numpy.finfo.html)).
- safety (float) - RKQS control safety factor $S$ (default 0.9).
- pgrow (float) - RKQS control growth exponent $P_{\text {grow }}$ (default -0.2).
- pshrink (float) - RKQS control shrinkage exponent $P_{\text {shrink }}$ (default -0.25 ).
- maxgrow (float) - RKQS control maximum factor to grow step size $f_{\max }$ (default 5).
- minshrink (float) - RKQS control minimum factor to shrink step size $f_{\min }$ (default 0.1 ).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import PseudoRKQSStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\max }$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, | new - old । / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> old = -1.
>>> stepper = PseudoRKQSStepper(start=0., stop=totaltime, inclusive=True,
... record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
... error = abs(new - old) / errorscale
...
    if step.succeeded(value=new, error=error):
        old = new
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
    len(stepper.steps)))
346 succesful steps in 361 attempts
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

Check that the post hoc error satisfies the desired tolerance.

```
>>> print(max(errors) < 1.)
True
```

346 successful PseudoRKQSStepper steps and trajectory of 361 attempts


## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded ().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.
property steps
ndarray of values of the control variable attempted so far.
succeeded (step, value $=$ None, error $=$ None )
Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional)-User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool
property successes
ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.scaledStepper

## Classes

class steppyngstounes.scaledStepper.ScaledStepper (start, stop, size=None, minStep=None, inclusive $=$ False, record $=$ False, growFactor $=1.2$, shrinkFactor $=0.5$ )
Bases: Stepper
Adaptive stepper that adjusts the step by fixed factors.
Calculates a new step as

$$
\Delta_{n+1}=f_{\text {grow }} \Delta_{n}
$$

where $\Delta_{n}$ is the step size for step $n$ and $f_{\text {grow }}$ is the factor by which to grow the step size.
On failure, retries with

$$
\Delta_{n}=f_{\text {shrink }} \Delta_{n}
$$

where $f_{\text {shrink }}$ is the factor by which to shrink the step size.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- size (float) - Suggested step size to try (default None).
- minStep (float) - Smallest step to allow (default (stop - start) * eps (https://numpy.org/doc/stable/reference/generated/numpy.finfo.html)).
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).
- growFactor (float) - Growth factor $f_{\text {grow }}$ (default 1.2).
- shrinkFactor (float) - Shrinkage factor $f_{\text {shrink }}$ (default 0.5 ).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import ScaledStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old । / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> old = -1.
>>> stepper = ScaledStepper(start=0., stop=totaltime, inclusive=True,
... record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
...
... error = abs(new - old) / errorscale
...
... if step.succeeded(value=new, error=error):
... old = new
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
... len(stepper.steps)))
296 succesful steps in 377 attempts
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

Check that the post hoc error satisfies the desired tolerance.

```
>>> print(max(errors) < 1.)
True
```


## 296 successful ScaledStepper steps and trajectory of 377 attempts



## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded ().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.
property steps
ndarray of values of the control variable attempted so far.

```
succeeded (step, value=None, error=None)
```

Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional)- User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which $S t e p p e r$ is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool
property successes
ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().
steppyngstounes.sequenceStepper

## Classes

class steppyngstounes.sequenceStepper. SequenceStepper (start, stop, sizes, inclusive=False, record=False)
Bases: Stepper
Stepper that takes a series of fixed steps.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- sizes (iterable of float) - Desired step sizes. In the event that start plus the sum of sizes will exceed stop, the stepper will terminate at stop.
- inclusive (bool) - Whether to include an evaluation at start (default False)
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).


## Examples

```
>>> import numpy as np
>>> from steppyngstounes import SequenceStepper
```

We'll demonstrate using an artificial function that changes abruptly, but smoothly, with time,

$$
\tanh \frac{\frac{t}{t_{\max }}-\frac{1}{2}}{2 w}
$$

where $t$ is the elapsed time, $t_{\text {max }}$ is total time desired, and $w$ is a measure of the step width.

```
>>> totaltime = 1000.
>>> width = 0.01
```

The scaled "error" will be a measure of how much the solution has changed since the last step, I new - old | / errorscale).

```
>>> errorscale = 1e-2
```

Iterate over the stepper from start to stop (inclusive of calculating a value at start).

```
>>> stepper = SequenceStepper(start=0., stop=totaltime, inclusive=True,
... sizes=range(1,10000), record=True)
>>> for step in stepper:
... new = np.tanh((step.end / totaltime - 0.5) / (2 * width))
...
... - = step.succeeded(value=new)
```

```
>>> s = "{} succesful steps in {} attempts"
>>> print(s.format(stepper.successes.sum(),
... len(stepper.steps)))
4 6 \text { succesful steps in 46 attempts}
```

```
>>> steps = stepper.steps[stepper.successes]
>>> ix = steps.argsort()
>>> values = stepper.values[stepper.successes][ix]
>>> errors = abs(values[1:] - values[:-1]) / errorscale
```

As this stepper doesn't use the error, we don't expect the post hoc error to satisfy the tolerance.

## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

46 successful SequenceStepper steps and trajectory of 46 attempts


## Return type

Step

## Raises

StopIteration - If there are no further steps to take

## property sizes

ndarray of the step size at each step attempt.

## property steps

ndarray of values of the control variable attempted so far.
succeeded (step, value=None, error=None)
Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional)- User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool

## property successes

ndarray of whether the step was successful at each step attempt.
property values
ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

## steppyngstounes.stepper

## Classes

```
class steppyngstounes.stepper.Step (begin, end, stepper, want)
```

Bases: object
Object describing a step to take.

## Parameters

- begin (float) - The present value of the variable to step over.
- end (float) - The desired value of the variable to step over.
- stepper (Stepper) - The adaptive stepper that generated this step.
- want (float) - The step size really desired if not constrained by, e.g., end of range.

```
succeeded ( value=None, error=None)
```

Test if step was successful.

## Parameters

- value (float, optional)- User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful. If error is not required, returns True.

## Return type

bool
class steppyngstounes.stepper.Stepper (start, stop, size $=$ None, minStep $=$ None, inclusive $=$ False, record $=$ False, limiting $=$ False )

Bases: object
Adaptive stepper base class.

## Parameters

- start (float) - Beginning of range to step over.
- stop (float) - Finish of range to step over.
- size (float) - Suggested step size to try (default None).
- minStep (float) - Smallest step to allow (default (stop - start) * eps (https://numpy.org/doc/stable/reference/generated/numpy.finfo.html)).
- inclusive (bool) - Whether to include an evaluation at start (default False).
- record (bool) - Whether to keep history of steps, errors, values, etc. (default False).
- limiting (bool) - Whether to prevent error from exceeding 1 (default False).


## property errors

ndarray of the "error" at each step attempt.
The user-determined "error" scalar value (positive and normalized to 1 ) at each step attempt is passed to Stepper via succeeded().
next ()
Return the next step.

Note: Legacy Python 2.7 support.

## Return type

Step

## Raises

StopIteration - If there are no further steps to take

```
property sizes
```

ndarray of the step size at each step attempt

## property steps

ndarray of values of the control variable attempted so far.
succeeded (step, value $=$ None, error=None)
Test if step was successful.
Stores data about the last step.

## Parameters

- step (Step) - The step to test.
- value (float, optional) - User-determined scalar value that characterizes the last step. Whether this parameter is required depends on which Stepper is being used. (default None).
- error (float, optional) - User-determined error (positive and normalized to 1) from the last step. Whether this parameter is required depends on which Stepper is being used. (default None).


## Returns

Whether step was successful.

## Return type

bool

```
property successes
```

ndarray of whether the step was successful at each step attempt.

## property values

ndarray of the "value" at each step attempt.
The user-determined scalar value at each step attempt is passed to Stepper via succeeded ().

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## Python Module Index

```
S
steppyngstounes,5
steppyngstounes.checkpointStepper, 5
steppyngstounes.fixedStepper,8
steppyngstounes.parsimoniousStepper,11
steppyngstounes.pidStepper,14
steppyngstounes.pseudoRKQSStepper, 18
steppyngstounes.scaledStepper, 21
steppyngstounes.sequenceStepper, 24
steppyngstounes.stepper, 27
```


## Index

C
CheckpointStepper (class in steppyngstounes.checkpointStepper), 5

## E

next () (steppyngstounes.scaledStepper.ScaledStepper method), 23
next () (steppyngstounes.sequenceStepper.SequenceStepper method), 25
next () (steppyngstounes.stepper.Stepper method), 28
errors (steppyngstounes.checkpointStepper.CheckpointStepp $\Phi$ property), 6
errors (steppyngstounes.fixedStepper.FixedStepper prop- ParsimoniousStepper (class in steppynerty), 9
errors (steppyngstounes.parsimoniousStepper.Parsimonious§teppert epper (class in steppyngstounes.pidStepper), 14
property), 13
PseudoRKQSStepper (class in steppyn-
errors (steppyngstounes.pidStepper.PIDStepper prop-
erty), 16
errors (steppyngstounes.pseudoRKQSStepper.PseudoRKQSSTEpper
property), 20 ScaledStepper (class in steppyn-
errors (steppyngstounes.scaledStepper.ScaledStepper
property), 23
errors (steppyngstounes.sequenceStepper.SequenceStepper property), 25
errors (steppyngstounes.stepper.Stepper property), 28

## F

FixedStepper (class in steppyngstounes.fixedStepper), 8

## M

module
steppyngstounes, 5
steppyngstounes.checkpointStepper, 5
steppyngstounes.fixedStepper, 8
steppyngstounes.parsimoniousStepper,
11
steppyngstounes.pidStepper, 14
steppyngstounes.pseudoRKQSStepper, 18
steppyngstounes.scaledStepper, 21
steppyngstounes.sequenceStepper, 24
steppyngstounes.stepper, 27

## N

next () (steppyngstounes.checkpointStepper.CheckpointStepper
method), 6
next () (steppyngstounes.fixedStepper.FixedStepper method), 9 gstounes.parsimoniousStepper), 11
gstounes.scaledStepper), 21
SequenceStepper (class in steppyn-
gstounes.sequenceStepper), 24
sizes (steppyngstounes.checkpointStepper.CheckpointStepper property), 8
sizes (steppyngstounes.fixedStepper.FixedStepper property), 11
sizes (steppyngstounes.parsimoniousStepper.ParsimoniousStepper property), 13
sizes (steppyngstounes.pidStepper.PIDStepper property), 16
sizes (steppyngstounes.pseudoRKQSStepper.PseudoRKQSStepper property), 21
sizes (steppyngstounes.scaledStepper.ScaledStepper property), 24
sizes (steppyngstounes.sequenceStepper.SequenceStepper property), 27
sizes (steppyngstounes.stepper.Stepper property), 28
Step (class in steppyngstounes.stepper), 27
Stepper (class in steppyngstounes.stepper), 28
steppyngstounes module, 5
steppyngstounes.checkpointStepper module, 5
steppyngstounes.fixedStepper module, 8
steppyngstounes.parsimoniousStepper module, 11
steppyngstounes.pidStepper
next () (steppyngstounes.parsimoniousStepper.ParsimoniousStepperodule, 14 method), 13
next () (steppyngstounes.pidStepper.PIDStepper method), 16
steppyngstounes.pseudoRKQSStepper module, 18
steppyngstounes.scaledStepper
next () (steppyngstounes.pseudoRKQSStepper.PseudoRKQSSteppermodule, 21
method), 20

```
    module,24 property),27
steppyngstounes.stepper successes (steppyngstounes.stepper.Stepper property),
    module, 27
    29
steps (steppyngstounes.checkpointStepper.CheckpointStepper 
steps (steppyngstounes.fixedStepper.FixedStepper prop- values (steppyngstounes.checkpointStepper.CheckpointStepper
        erty),11 property), 8
```



```
    property),14 erty), 11
steps (steppyngstounes.pidStepper.PIDStepper property), values (steppyngstounes.parsimoniousStepper.ParsimoniousStepper
    1 6 ~ p r o p e r t y ) , 1 4
steps(steppyngstounes.pseudoRKQSStepper.PseudoRKQSStepmeerues (steppyngstounes.pidStepper.PIDStepper prop-
    property),21 erty),18
steps(steppyngstounes.scaledStepper.ScaledStepper prop- values(steppyngstounes.pseudoRKQSStepper.PseudoRKQSStepper
            erty), 24
steps (steppyngstounes.sequenceStepper.SequenceStepper
        property), 27
steps (steppyngstounes.stepper.Stepper property), 29
succeeded() (steppyn-
    gstounes.checkpointStepper.CheckpointStepper
    method), }
succeeded() (steppyn-
    gstounes.fixedStepper.FixedStepper method),
    11
succeeded() (steppyn-
    gstounes.parsimoniousStepper.ParsimoniousStepper
    method),14
succeeded() (steppyngstounes.pidStepper.PIDStepper
    method),16
succeeded() (steppyn-
    gstounes.pseudoRKQSStepper.PseudoRKQSStepper
    method), 21
succeeded() (steppyn-
    gstounes.scaledStepper.ScaledStepper method),
    24
succeeded() (steppyn-
    gstounes.sequenceStepper.SequenceStepper
    method),27
succeeded() (steppyngstounes.stepper.Step method), 27
succeeded() (steppyngstounes.stepper.Stepper method),
    29
successes (steppyngstounes.checkpointStepper.CheckpointStepper
    property), }
successes (steppyngstounes.fixedStepper.FixedStepper
    property),11
successes (steppyngstounes.parsimoniousStepper.ParsimoniousStepper
    property),14
successes (steppyngstounes.pidStepper.PIDStepper
    property),18
successes(steppyngstounes.pseudoRKQSStepper.PseudoRKQSStepper
    property),21
successes (steppyngstounes.scaledStepper.ScaledStepper
    property), }2
successes (steppyngstounes.sequenceStepper.SequenceStepper
```


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